## Math 313 Exam 2 competencies

## **Exam Content**

This exam will cover material specifically from sections 2.1-2.3, 3.1-3.3, and 4.1-4.4. There will be two types of questions: multiple choice and free response. The format of the exam will be similar to exam 1.

## Specific Learning Outcomes for Exam 1

- 1. Know how to calculate matrix operations, such as scalar multiplication, matrix addition, matrix vector multiplication, and matrix-matrix multiplication. Know the properties.
- 2. Be able to tell when matrix addition or multiplication is valid.
- 3. Know the meaning of "Matrix multiplication is not commutative", and be able to give examples.
- 4. Know how to construct Elementary matrices, and their inverses.
- 5. Know the theorems on invertible matrices.
- 6. Know how to find the inverse of a matrix using Gaussian Elimination.
- 7. Know how to use inverses to solve systems of equations.
- 8. Know the equivalencies in the Invertible Matrix Theorem.
- 9. Be able to use the Invertible Matrix theorem to deduce properties about a specific matrix.
- 10. Know what is meant by an invertible linear transformation.
- 11. Be able to tell when a linear transformation is invertible and be able to find the inverse transformation.
- 12. Know what is meant by  $A_{ij}$ , and what a cofactor is.
- 13. Be able to calculate the determinant of any matrix by expansion along a row or column.
- 14. Be able to calculate the determinant of a triangular or diagonal matrix.
- 15. Understand how row operations affect the determinant.
- 16. Be able to calculate the determinant of a matrix using row operations.
- 17. Understand the theorems regarding determinants.
- 18. Know what is meant by the adjoint of A.
- 19. Be able to calculate the inverse from the determinant and the adjoint.

- 20. Be able to use Cramer's rule to solve a system of equations.
- 21. Know the ten properties that define a vector space.
- 22. Be able to determine if a set with a defined addition and scalar multiplication is a vector space.
- 23. Know the vector spaces defined in class and in the book.
- 24. Know the properties of a vector space.
- 25. Know what is meant by a subspace.
- 26. Be able to determine if a particular subset of a vector space is a subspace.
- 27. Know the properties of subspaces.
- 28. Know what is meant by Nul(A) and Col(A).
- 29. Be able to find a basis for both Nul(A) and Col(A).
- 30. Understand what is meant by the kernel and range of a linear transformation and how they relate to the above spaces.
- 31. Be able to determine if a set of vectors in a vector space is linearly independent or linearly dependent.
- 32. Know the properties of linearly independent or dependent sets.
- 33. Know what is meant by a basis.
- 34. Be able to determine if a specific set in a Vector space is a basis.
- 35. Know and be able to apply the spanning set theorem.
- 36. Be able to write any vector in a vector space (not just  $\mathbb{R}^n$ ) in its coordinate vector from a basis.
- 37. Be able to construct the change of basis matrix from any basis to the standard basis.
- 38. Be able to determine properties of vectors in a vector space by examining their coordinates.